

Modal Analysis of Un-Crack and Crack Cantilever Beam Using FEA

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Abstract

In this paper, the present work deals with modal analysis of uncrack and crack cantilever beam using FEA. Faulty structure subjected to change in local flexibility which affects vibration response of the structure. Therefore it is necessary to study the effect of fault on the structure. In this paper, aluminum un-crack and crack cantilever beam is used for analysis. Un-crack beam and cracked beam analyzed by using Euler equation considering various crack positions for the beam. Modal analysis of un-crack and crack beam is performed to find deflection and natural frequencies of beam. The results are presented in tabular form to show the effect of crack on change in natural frequencies. ANSYS software was used for the analysis of un-crack and crack beam.

Keywords: *Cantilever beam, Modal Analysis, ANSYS.*

INTRODUCTION

Vibration in engineering structure causes the breakdown of the structures. Motion which repeats itself after a certain interval of time is called vibration. An unbalanced force created due to fault occurs into structure which causes to induced vibrations. Engineer's important task is to

Determine the effect of these damages on the stability characteristic of these structures. Fault leads to reduction in stiffness also with an inherent reduction in natural frequency and increase in modal damping. The study of vibration analysis of cantilever beam with crack is a problem of practical interest and finds applications in

aerospace, mechanical and civil engineering. Health monitoring and the analysis of damage in the form of crack in beam structures possess a vital mean.

In the literature, several studies deal with the effect of crack, crack detection by various methods.

Yang et al. performed the analytical study on the free and forced vibration of inhomogeneous Euler- Bernoulli beams containing open edge cracks. Analytical solutions were obtained for cantilever, with different end conditions to evaluate the dynamic response of the beam due to the edge crack.

Salawu and Williams presented an excellent review on the use of modal frequency changes for damage diagnostics. The observation that changes in structural properties cause changes in vibration frequencies was the impetus for using modal methods for damage identification and health monitoring.

The free and forced vibration analysis of a cracked beam was performed by S Orhan et al in order to identify the cracks in a cantilever beam. The study results suggest

that free vibration analysis provides suitable information for the detection of single and two cracks. The Euler- Bernoulli beam model was assumed for the analysis.

R. Tiwari and M. Karthikey developed identification procedure for the detection, localization, and size of a crack in a beam based on forced response measurements. E Cam, S Orhan et. al used the impact echo method for the analysis of cracked beam structure. They analyzed vibrations as a result of impact shocks. ANSYS software was used for validation of results and simulations.

Kim and Zhao proposed a novel crack detection method using harmonic response. They conclude that slope response has a sharp change with the crack location and depth of the crack, and therefore it can be used as a crack detection criterion.

S. Loutridis, E.Douk developed new method for crack detection in beams based on instantaneous frequency and empirical mode decomposition. It follows that the harmonic distortion increases with crack depth following definite trends and can be also used as an effective indicator for crack size.

Saavedra and Cuitio has performed the theoretical and experimental dynamic behaviors of different multi beams systems containing a transverse crack. In their analysis an analytical model of a cracked cantilever beam has been utilized, and natural frequencies are obtained through numerical methods. A genetic algorithm is utilized to monitor the possible changes in the natural frequencies of the structure.

Zheng and Kessissoglou have presented a method based on finite element method for detection of crack in faulty structural member. The results obtained from the proposed method are validated using experimental analysis.

In this paper Euler- Bernoulli beams is analyzed. First the natural frequency and deflection of Un-crack and crack cantilever beam is obtained using ANSYS with various conditions of beam with crack. The paper gives the effect of crack on natural frequency and deflection of beam with crack depth at different location. The study implies how natural frequency and deflection changes as the structure affected due to damage.

THEORY

The stability and local flexibility of the beam depends on the material properties, physical dimensions, boundary conditions of the structure which play important role for the determination of its dynamic response. The characteristics of beam greatly depend on the position of crack, depth of crack, orientation of crack and number of cracks.

The beam with rectangular crack is clamped at left end and free at right end and uniform in rectangular cross section along its length. The crack is assumed to be open crack and no damping is considered in this study.

Governing Equation for Free Vibration of Beam:

The differential equation for transverse vibration of thin uniform beam is obtained with the help of strength of materials. The beam has cross section area A , flexural rigidity EI and density of material ρ .

Consider the small element dx of beam is subjected to shear force Q and bending moment M , as shown in figure

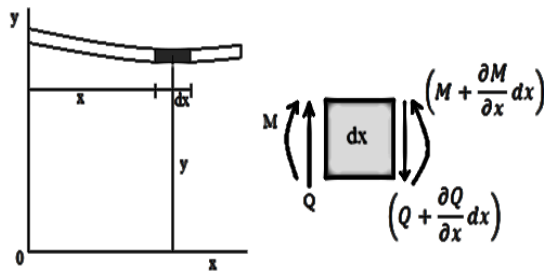
While deriving mathematical expression for transverse vibration, it is assumed that there

are no axial forces acting on the beam and effect of shear deflection is neglected. The deformation of beam is assumed due to moment and shear force.

The net force acting on the element,

$$Q - \left(Q + \frac{\partial Q}{\partial x} dx \right) = dm * \text{acceleration}$$

$$-\frac{\partial Q}{\partial x} dx = (\rho A dx) \frac{\partial^2 y}{\partial t^2}$$



**Fig.1. Shear Force and Bending Moment
acting on beam element**

$$\frac{\partial Q}{\partial x} + \rho A \frac{\partial^2 y}{\partial t^2} = 0$$

Considering the moments about A, we get

$$M - \left(M + \frac{\partial M}{\partial x} dx \right) + \left(Q + \frac{\partial Q}{\partial x} dx \right) dx = 0$$

$$-\frac{\partial M}{\partial x} + Q + \frac{\partial Q}{\partial x} dx = 0$$

So $Q = \frac{\partial M}{\partial x}$ higher order derivatives are neglected here $\left(\frac{\partial Q}{\partial x} dx = 0 \right)$

Or

$$\frac{\partial Q}{\partial x} = \frac{\partial^2 M}{\partial x^2}$$

From the above two equations 1 and 2, we get

$$\frac{\partial^2 M}{\partial x^2} = \rho A \frac{\partial^2 y}{\partial t^2}$$

We know from strength of materials that

$$M = -EI \frac{\partial^2 y}{\partial x^2}$$

So

$$\frac{\partial^2 M}{\partial x^2} = -EI \frac{\partial^4 y}{\partial x^4}$$

Comparing equation 3 and 4 we get,

$$\frac{\partial^4 y}{\partial x^4} + \left(\frac{\rho A}{EI} \right) \frac{\partial^2 y}{\partial t^2} = 0$$

This is the general equation for transverse vibration. Thus the natural frequency can be found out by this theory as,

$$\omega_n = C * \sqrt{\frac{EI}{\rho A l^4}}$$

Where,

E= Young's modulus of the material,

I= Moment of inertia,

A= Area of cross section,

l=length of the beam,

C= Constant depending mode of vibration,

C1=0.56 for first mode,

C2= 3.52 for second mode,

C3= 9.82 for third mode.

The moment of inertia can be found out by relation,

$$I = \frac{bd^3}{12}$$

Where,

b= width of the beam,

d= depth of the beam.

Due to presence of crack, moment of inertia of the beam changes and correspondingly the natural frequency also changes. For a constant beam material and cross section the

reduced moment of inertia will be found by relation below.

$$I_1 = I - I_c$$

Where,

I1=Moment of inertia of a cracked beam,

I=Moment of inertia of Uncracked beam,

Ic=Moment of inertia of cracked beam element.

Thus by the use of above equation, we can find out the different modes of natural frequencies for the cantilever beam.

CRACK CONFIGURATIONS

In this study, modal analysis of an aluminium cantilever beam having a rectangular crack is studied. The dimension of the beam is 400*30*5 mm. The material properties , modulus of elasticity (E) is 70*10⁹ N/m², the density (ρ) 2700 kg/m³, poisson's ration (μ) 0.3.

The various crack configurations of beam as are prepared to find how the crack affects the original characteristics of beam. Crack location at 100mm and 200mm with crack depth 1mm and 2mm are investigated to find deflection and natural frequency.

FINITE ELEMENT ANALYSIS

The ANSYS 14.5 was used for modal analysis of un cracked and cracked beams. In pre-processor, first the eight key points were crated and then straight line segments were formed. These straight lines were joined sequentially to create an area. Finally, the area was extruded along the normal plane and a three dimensional un crack and crack beam model was obtained

in ANSYS as shown in Fig.3 and Fig.4. A three dimensional SOLID 185 element was selected to model the beam. Crack beam was mesh using tetrahedral element which is the best for crack configuration. The first three natural frequencies for each case were obtained. Cantilever boundary conditions were modelled by constraining all degrees of freedoms on the left end area.

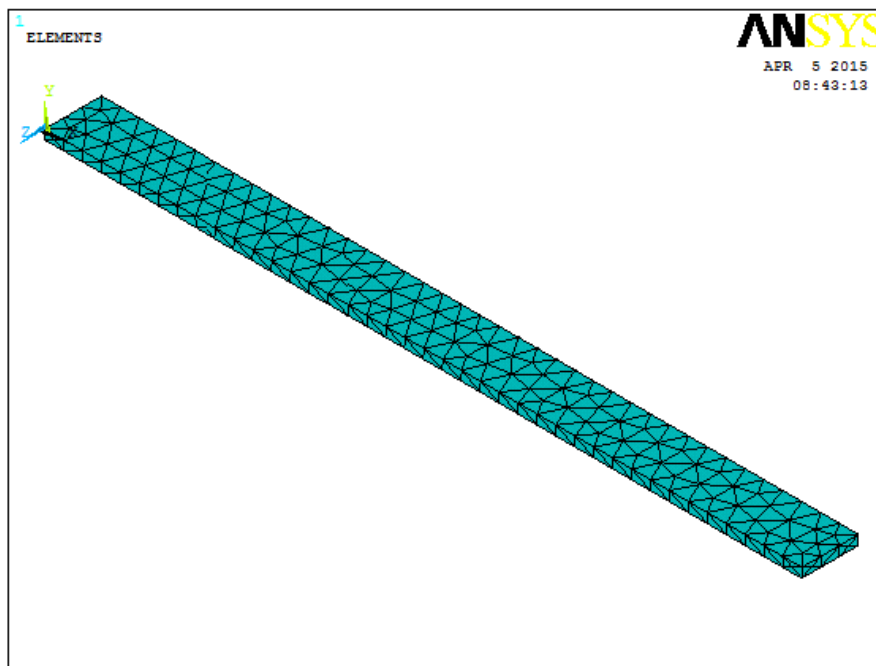


Fig.3 Cantilever Un crack Beam

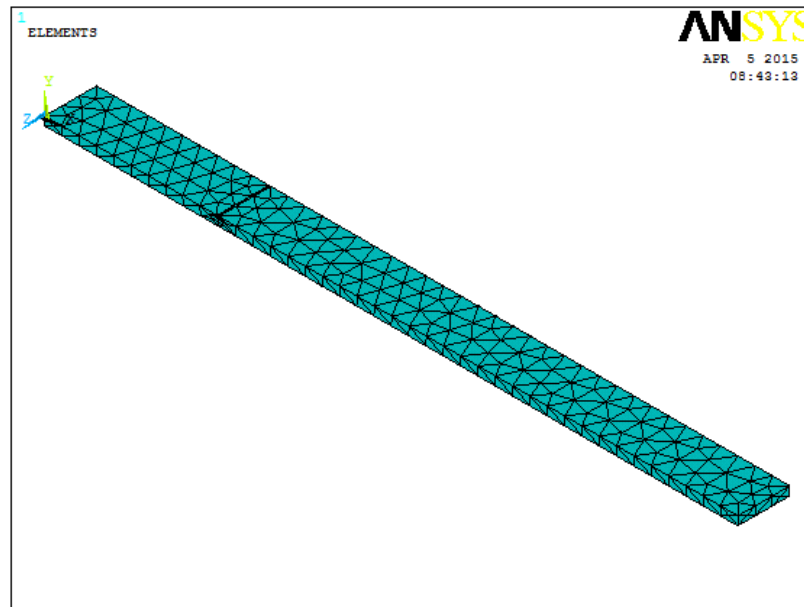


Fig.4 Cantilever Crack Beam

RESULTS & DISCUSSIONS

Table -1 Natural Frequency of Beam at Various Conditions

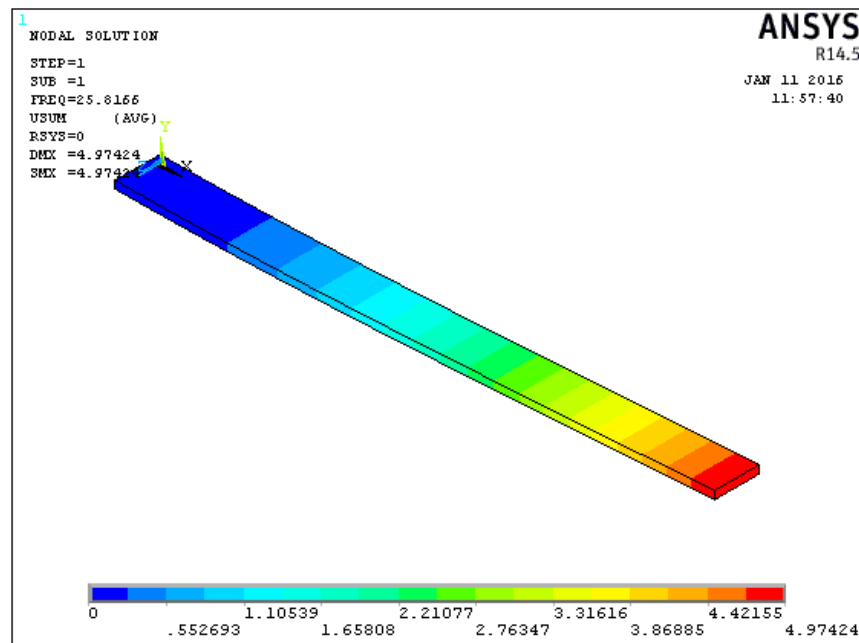
Beam Conditions		Beam without Crack	Crack Beam 1 mm depth & 100 mm length	Crack Beam 1 mm depth & 200 mm length	Crack Beam 2 mm depth & 100 mm length	Crack Beam 2 mm depth & 200 mm length
Natural Frequency in Hz	First	25.8166	46.3781	46.5864	45.709	47.0505
	Second	161.731	292.934	288.575	292.113	286.259
	Third	452.894	812.905	818.833	804.772	821.55

Modal analysis of un crack and crack cantilever beam was done for various condition of beam at various crack depth and locations to obtain deflection and natural frequencies.

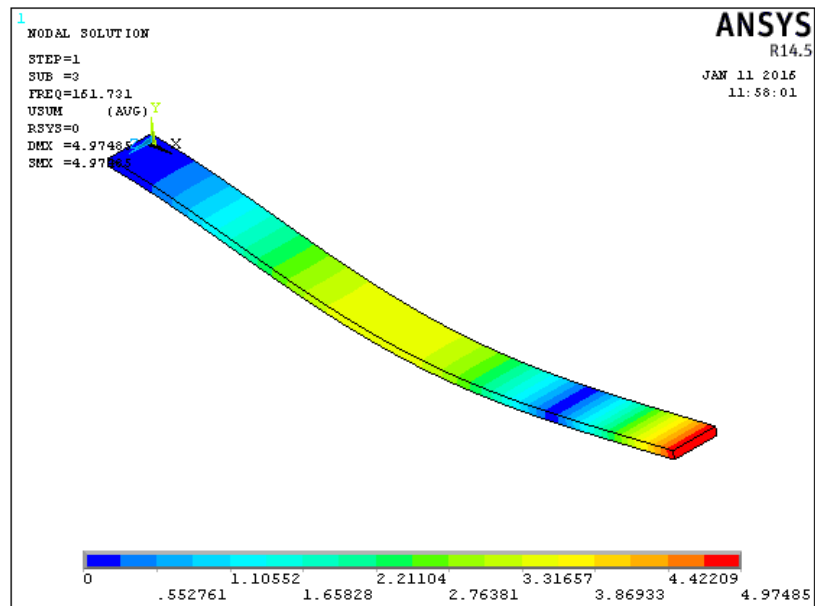
The change in natural frequencies with and without crack at various conditions of beam as shown in Table1. The natural frequency

of the crack beam the larger than uncrack beam. In uncrack beam natural frequencies decreases, in increase in crack depth at the same location.

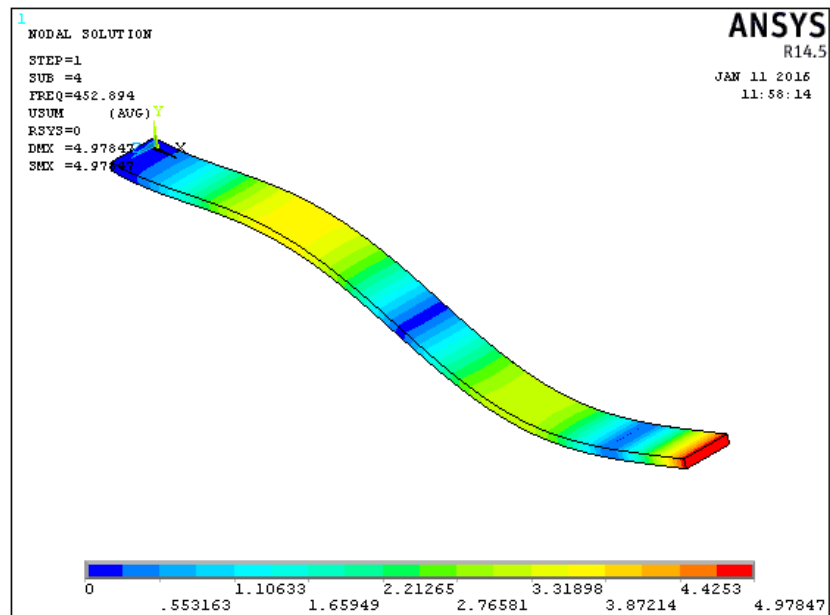
Natural Frequency of Cantilever Beam:



First Mode

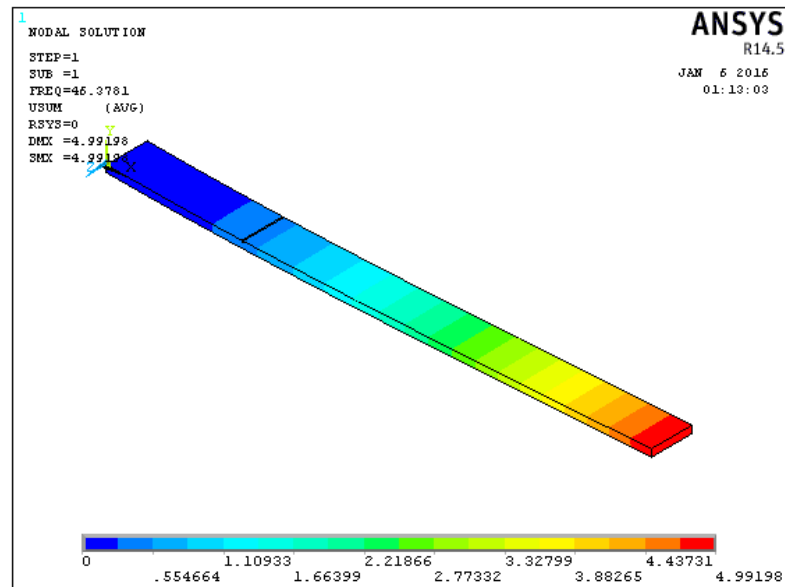


Second Mode

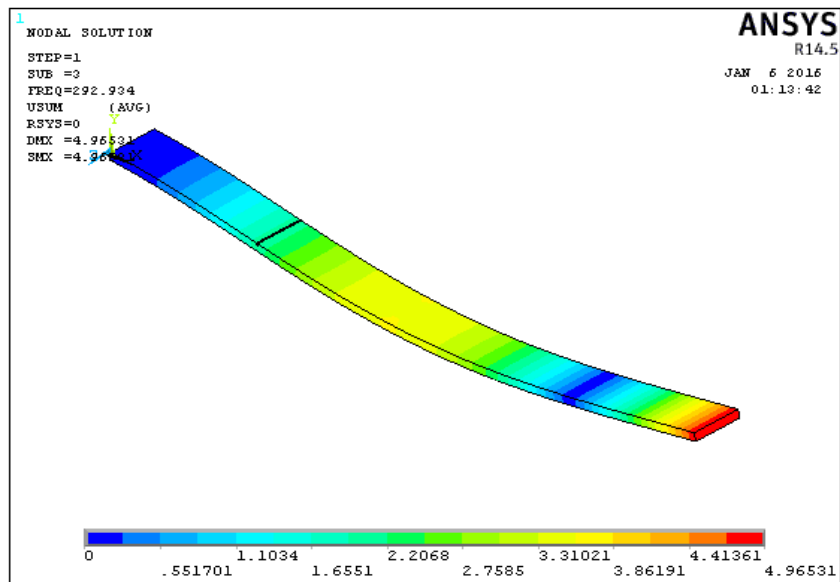


Third Mode

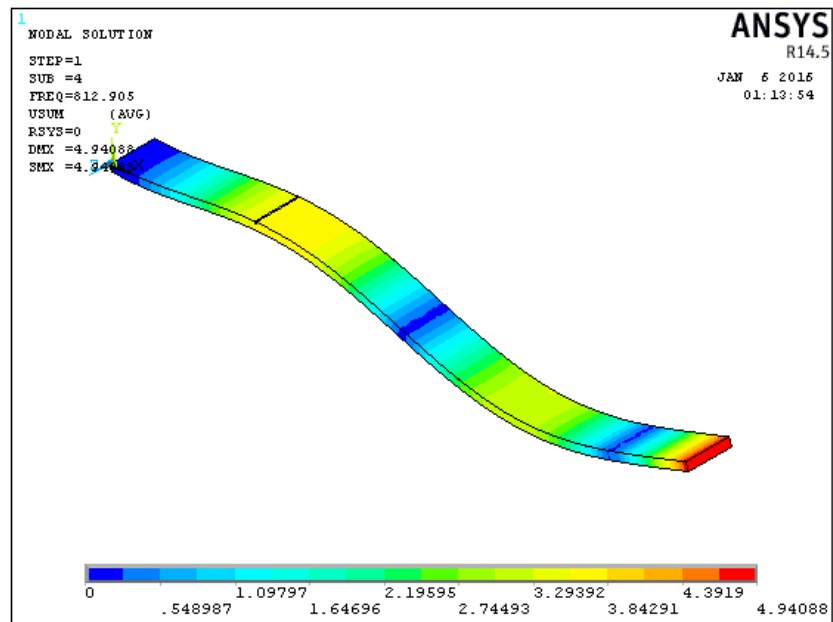
Crack Cantilever Beam with 1 mm Depth and 100 mm Lengths:



First Mode

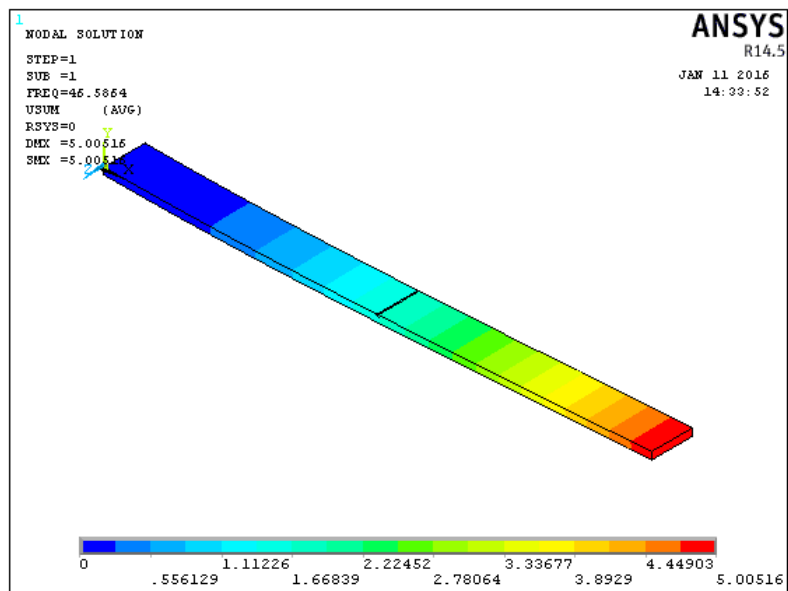


Second Mode

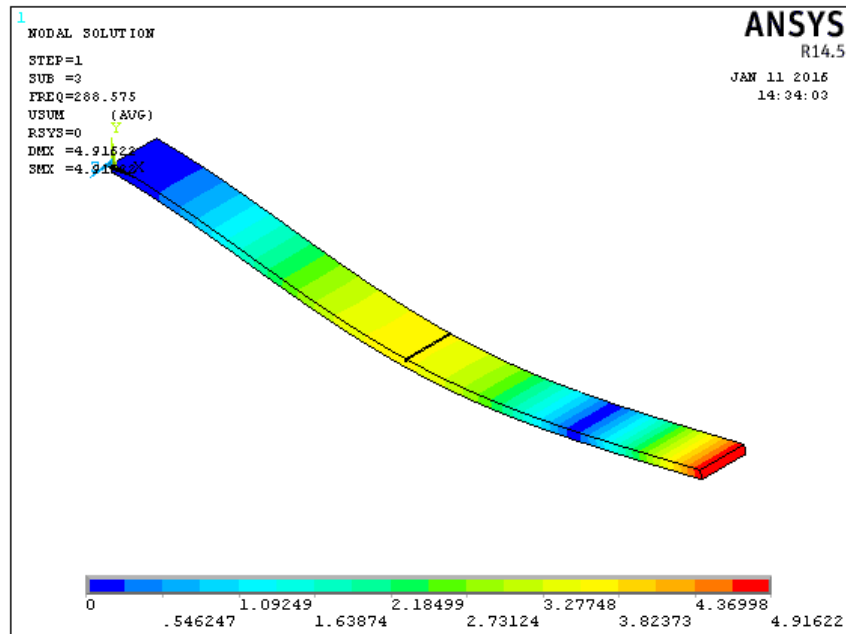


Third Mode

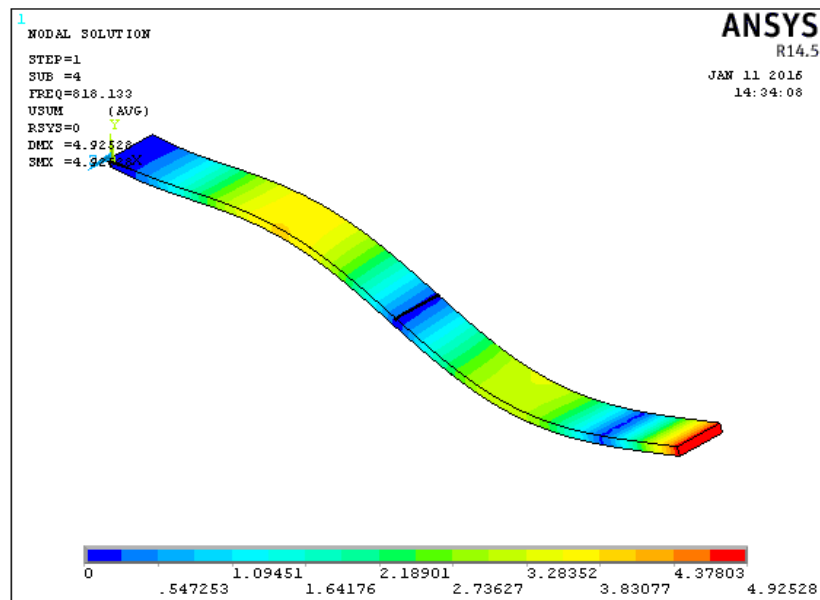
Crack Cantilever Beam with 1 mm Depth and 200 mm Lengths:



First Mode

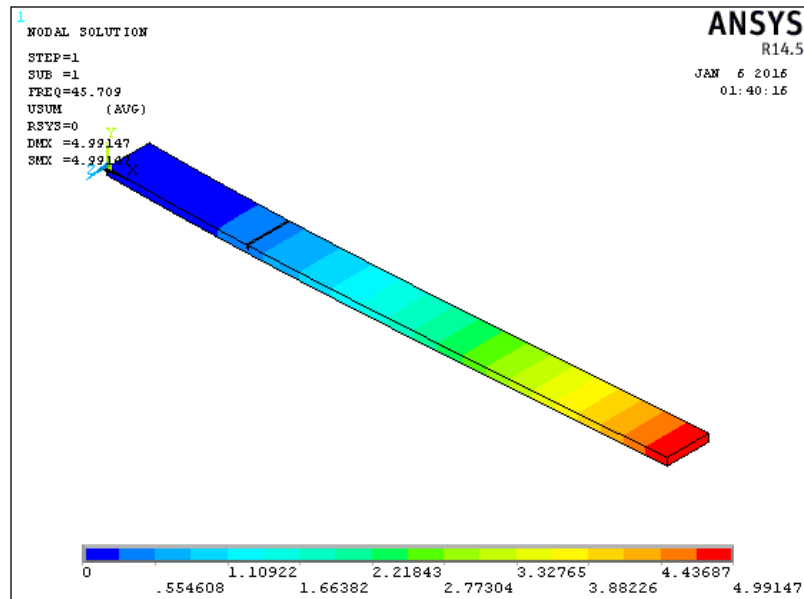


Second Mode

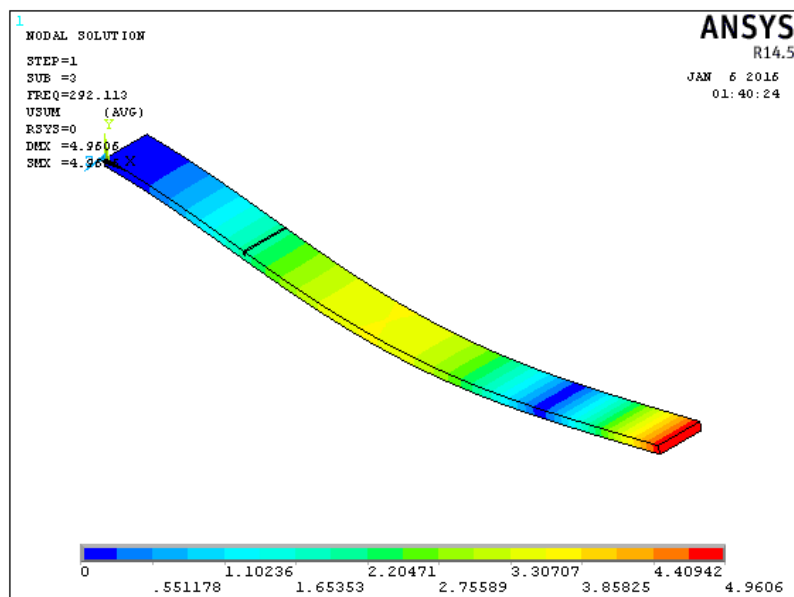


Third Mode

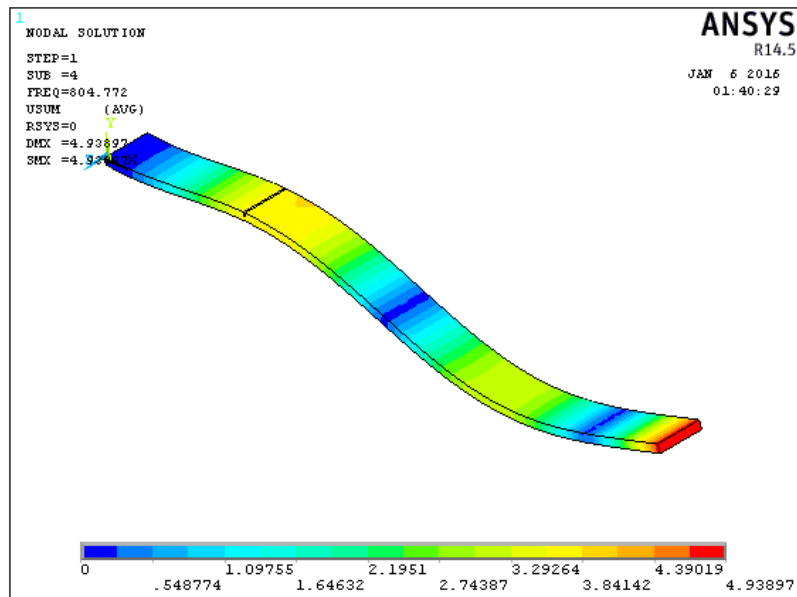
Crack Cantilever Beam with 2 mm Depth and 100 mm Lengths:



First Mode

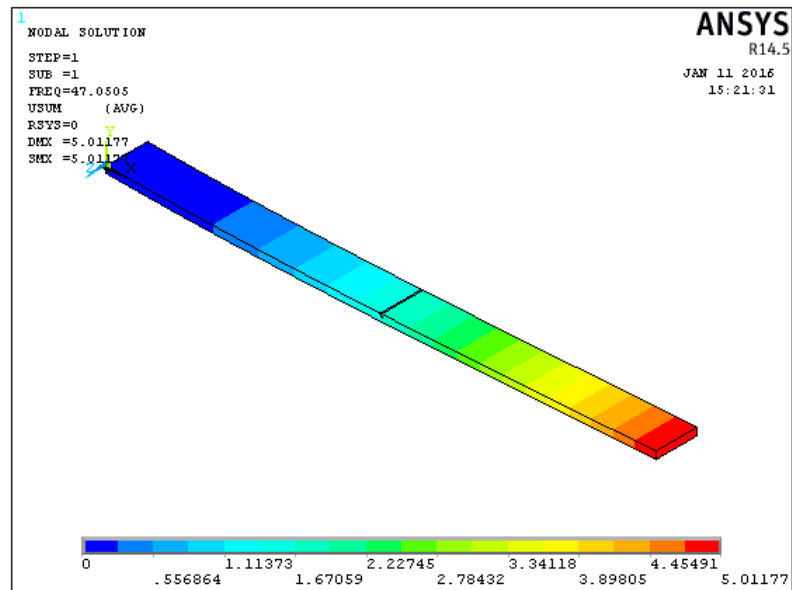


Second Mode

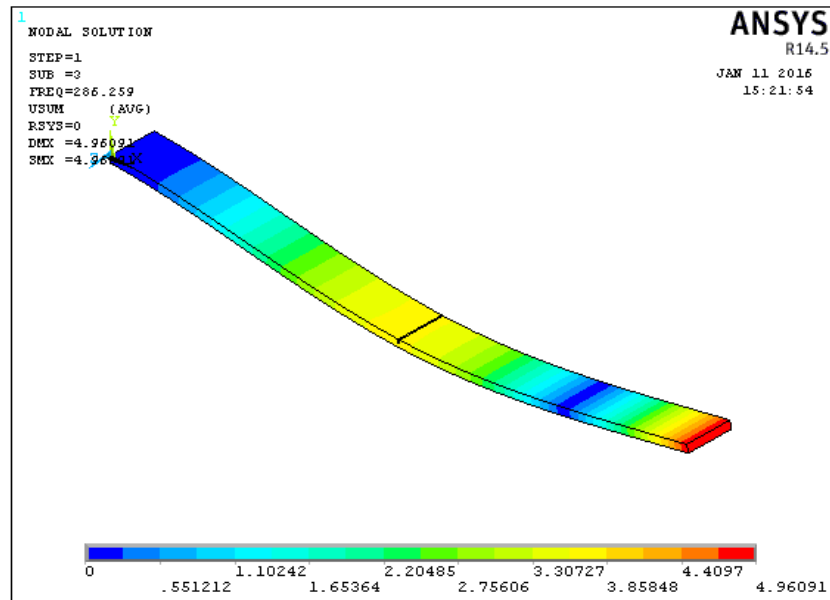


Third Mode

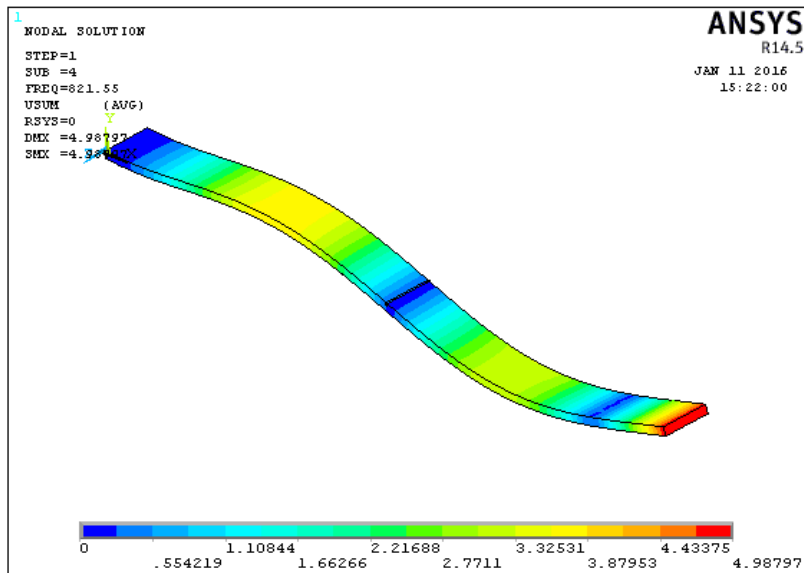
Crack Cantilever Beam with 2 mm Depth and 200mm Length:



First Mode



Second Mode



Third Mode

CONCLUSION

In the present section, the natural frequency of beam is calculated using ANSYS. Results obtained from the various analyses can be concluded as follows:

The natural frequency of the crack beam is larger than uncrack beam for same c/s .

For crack beam: At same location - natural frequency decreases, in increase in the crack depth.

At increase in crack location- natural frequency increases, with same crack depth.

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