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Comparison of Different Techniques of PAPR Reduction in OFDM System

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Abstract

Orthogonal frequency division multiplexing (OFDM) is a well-organized frequently used multicarrier modulation method for high speed data communication over multipath fading channels. OFDM modulation technique offer many benefits for multicarrier transmission at high information rates. One of the major limitations of OFDM is high peak to-average power ratio (PAPR) of the transmitted signal that badly influences the complexity of high power amplifier. Various promising procedures have been anticipated and implemented to decrease PAPR of OFDM signal at the outlay of transmitted signal power, bit error rate (BER), complexity and so on. In this paper, Clipping and Filtering, Selective Mapping (SLM), Partial Transmits Sequence (PTS), tone insertion and tone reservation techniques are discussed briefly for PAPR reduction OFDM signal at transmitter. A brief comparison of these PAPR reduction techniques is done in light of CCDF and BER

Keywords: *OFDM System, PAPR reduction, Bit error rate (BER), Selective Mapping (SLM), Partial Transmits Sequence (PTS)*

INTRODUCTION

Mobile radio communication systems are gradually required to offer a variety of brilliant multi-media services to mobile users. To meet these demands in far-flung broadband communication systems must

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have the capacity to support high limit, variable bit rate data transmission and high data transfer capacity effectiveness. In the mobile radio condition, signals are normally disabled by fading and what's more, multi-path delay phenomenon. In these channels, severe fading of the signal amplitude and inter symbol interference (ISI) due to frequency selectivity of the channel bring about an incompatible degradation of the error performance.

Orthogonal frequency division multiplexing (OFDM) is a multi-carrier modulation scheme for high data rate mobile communication system because of its vigor to frequency selective fading, high spectral efficiency and low computational complexity. Recently OFDM system has been getting across the board consideration. Orthogonal frequency division multiplexing can be used in conjunction with multiple-input multiple-output (MIMO) method to enhance diversity gain and/or the system capacity by exploiting spatial domain.

MIMO-OFDM is viewed as a key innovation in rising high data-rate communication system, including digital subscriber lines (DSL), IEEE 802. l1, IEEE 802.16 and IEEE 802.15.3a, give a course to 4G technology that support high mobile data rates. The primary advantages of utilizing MIMO-OFDM technique, which can diminish the recipient unpredictability and manage the multipath fading effectively, incorporate high spectral efficiency and robustness against narrowband.

The fundamental points of interest of utilizing MIMO-OFDM procedures, which can diminish the recipient intricacy and manage the multipath fading effectively, incorporate high spectral efficiency and strength against narrowband interference, uniform average spectral density, capacity of dealing with exceptionally solid echoes, less non-linear distortion and efficient implementation. Notwithstanding, the principle limitation of utilizing MIMO-OFDM endures with the problem of high PAPR and carrier frequency offset sensitivity [6].

Subsequently, it is imperative to decrease the PAPR; otherwise, high power amplifier (HP A) in the transmitter need to have a linear region that is substantially bigger than the average power, which makes them costly and wasteful. This is because if HPA with a linear region somewhat more

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noteworthy than the average power is utilized, the saturation brought about by the vast peak will result in intermodulation distortion, which expands the bit error rate (BER) and causes spectral widening, bringing about adjacent channel interference.

A number of PAPR reduction techniques have been proposed to handle this problem. One of the most widely used strategies is Clipping and Filtering, DFT Spreading and Partial Transmit sequence (PTS), utilizing probabilistic techniques [3]. The guideline of probabilistic strategy relies on upon decreasing the likelihood of high PAPR by creating several OFDM symbols (multiple candidates) conveying a similar information and choosing the one having the most minimal PAPR [2]. The probabilistic technique can likewise be classified into two systems: sub block partitioning methodology and entire block procedure.

The sub block partitioning procedure, for example, partial transmit sequence (PTS) [8-9], separates frequency domain signals into several sub blocks. on the other hand, the entire block Strategy, for example, Clipping and Filtering, DFT Spreading, [5–8] consider the whole block for creating numerous candidates. To begin with, the entire block procedure of the probabilistic strategies to create numerous candidates is viewed as, and then the probability Distribution Function (PDF) for the multiple candidate system is investigated. When the candidate having the reduced APR is chosen, the PDF of the amplitude of a selected OFDM symbol becomes a function of the number of candidates

[1-4]. All through this paper we portray the fundamental rule of every one of these procedures. The determination of any of the PAPR reduction technique may be at the cost of PAPR reduction ability, synchronization between the transmitter and the receiver. The absence of the PAPR reduction techniques will cause the increase in the transmit power, bit error rate at the receiver, the data rate loss, and the computational complexity. Here we have studied through simulation result the performance of PTS and Clipping and Filtering, DFT Spreading based PAPR reduction techniques for these techniques in view of different parameters.

PRINCIPLE ALGORITHM FOR REDUCING PAPR

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An OFDM signal includes various independently modulated sub-carriers, which can give a considerable PAPR when added up coherently. At the point when N signals are added with the similar phase, they generate a peak power that is N times the average power of the signal. So OFDM signal has a substantial PAPR, which is sensitive to non-linearity of the high power amplifier. PAPR is a historic issue in the advancement of the Wireless communication, the more PAPR of OFDM the more prerequisites and difficulties for executing the HPA. However the PAPR is computed from the peak amplitude of the waveform divided by the average value of waveform as follows:

$$\text{PAPR} = \frac{maX_0 \le t \le nT\left|X_n\right|^2}{E\{\left|X_n\right|^2\}} \qquad 1$$

Where $E\{|x(t)|^2\}$ is average power of the waveform. The amplitude of the waveform has Rayleigh distribution. The distribution of PAPR states in term complementary cumulative distribution function (CCDF).

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$$\text{CCDF} = \Pr(\text{PAPR} < \text{PAPR}_0 = A) \qquad 2$$

Assume $\text{PAPR}_0 = A$

$$F_X(\text{PAPR}) = \Pr\left[\frac{maX_0 \le t \le nT\left|X_n\right|^2}{E\left\{\left|X_n\right|^2\right\}} \le PAPR_0\right]$$

$$= 1 - \exp(-\text{PAPR}_0) \qquad 3$$

$$\text{CCDF} = \Pr(\text{PAPR} > \text{PAPR}_0) = 1F_X(\text{PAPR}_0)^N$$

$$= 1 - (1-\exp(-\text{PAPR}_0))^N \qquad 4$$

The decibel form of equation (4) is as following:

$$\text{PAPR}_{dB} = 10\log_{10}(\text{PAPR}) \qquad 5$$

Despite the fact that the probability of the largest PAPR to happen is not high, but rather to send the high PAPR of OFDM signal with no distortion, the probability increases. All the linearity in High Power Amplifier (HPA) and A/D converter ought to meet the necessities said above [1-3]. Since the hardware that meets these necessities is exceptionally costly, therefore, it is extremely requesting and essential to reduce PAPR in OFDM system [9-10].

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PAPR AND ITS REDUCTION IN OFDM SYSTEM

A block diagram of OFDM system is delineated in Fig.1. The OFDM flag comprises of an sum of subcarriers that are modulated by phase shift keying (PSK) or Quadrature Amplitude modulation (QAM). To start with, the serial input data stream is arranged into N group of bits, where Nc is the number of subcarriers. The number of bits in each of the Nc group decides the constellation size mea for that specific subcarrier. The mapped complex symbol are then serial- to-parallel (S/P) converted and oversampled by a factor L resulting in a block Nc L complex symbols [11].

The complex discrete time base band OFDM signal can be expressed as:

$$X_{N_T}(t) = \frac{1}{\sqrt{N}} \sum_{n=0}^{N-1} X_n e^{j2\pi F_n t}, 0 \le t \le nT \quad 6$$

Where NT transmit an antenna that make use of N subcarrier. By using OFDM modulation technique, a block of n data symbols (one OFDM symbol) {Xn , n=0,1….n-1} will be transmitted in parallel such that each symbol modulate a different carrier such that each modulates a different subcarrier from a set {fN , N = 0, 1… N-1}. The N subcarriers are orthogonal, that is fN= NΔf where Δf = 1/nT and T is the symbol time period. The above power attributes can likewise be portrayed regarding their magnitude (not power) by defining the crest factor (CF) as:

Pass Band and Condition: CF = $\sqrt{PAPR}$ 7

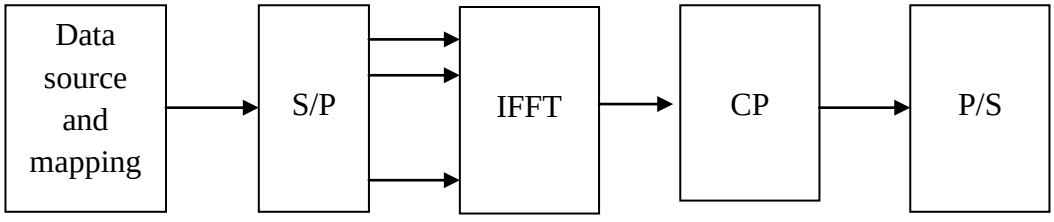


Figure1. Block diagram of OFDM system.

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In the PSK/OFDM system with N subcarriers, the most extreme power happens when the greater part of the N subcarrier components happen to be added with same phase. Assuming that $E\{|X_n|^2\} = 1$. It result in PAPR = N, that is the maximum power equivalent to N times the average power. We have noticed that when M-QAM is greater than 4 times M-PSK, the PAPR will be large in this case.

The Probability distribution of X_n will follow after the Gaussian distribution. The amplitude of OFDM signal has a Rayleigh distribution with zero mean and a variance of N times the variance of one complex sinusoid. let {Zn} be chance to be the extents of complex samples. Accepting that the average power of complex pass band OFDM signal X_n is equivalent to one, the {Zn} are the standardized Rayleigh arbitrary variable with its own average power, which has the probability density function [4-9] as shown below:

$$F_{z_n}(Z) = \frac{Z}{\sigma^2} e^{-Z^2} \Big/ 2\sigma^2 = 2Ze^{-Z^2} \qquad 8$$

Where $E\{|Z_n|^2\}=2\sigma$.

PAPR REDUCTION TECHNIQUES

Partial transmit sequence

The Partial Transmit Sequence has been presented by Muller and Hubber in 1997 [11]. The PTS technique is based on phase shifting of sub-block of data and then multiplication of data structure by random vectors. This technique is flexible and efficient for OFDM framework. A block diagram of PTS technique is shown in figure 2. In partial transmit sequence [12] the input data block of N symbols is further divided into V disjoint sub-blocks. The input data block can be written in form of X_V as:

$$X = \sum_{V=0}^{V-1} X_V \qquad 9$$

Each partitioned sub-block is multiplied by a corresponding complex phase factor bv= ejΦv , v = 1,2,….V then taking its IFFT to yield

$$X = IFFT\{\sum_{v=1}^{V} b^v X^v\} = \sum_{v=1}^{V} b^v IFFT\{X^v\} = \sum_{v=1}^{V} b^v X^v$$

Where Xv represent the partial transmit sequence. The value of phase vector is selected in such a manner that the value of resulted PAPR is minimized [12]. This is shown as

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$$\left[\tilde{b},.....\tilde{b}^{v}\right]=\left[b^{1},.....b^{v}\right]^{\arg\min\left(n=0,1,.....N-1\left|\max\sum_{v=1}^{V}b^{v}x^{v}[n]\right|\right)} \quad 11$$

Then the corresponding time domain signal with the lowest PAPR can be expressed as

$$X=\{\sum_{v=1}^{V}b^{v}X^{v}\}$$

In general the reduction in search complexity largely depends upon the selection of phase factor which is limited to a set of elements. As the set of allowed phase factors is

$$b=\{e^{j2\Pi i/w}\left|i=0,1,2,...w-1\right\}\ ,\mathrm{w}^{\mathrm{v-1}}$$

Therefore search complexity is directly proportional to the number of sub-block.

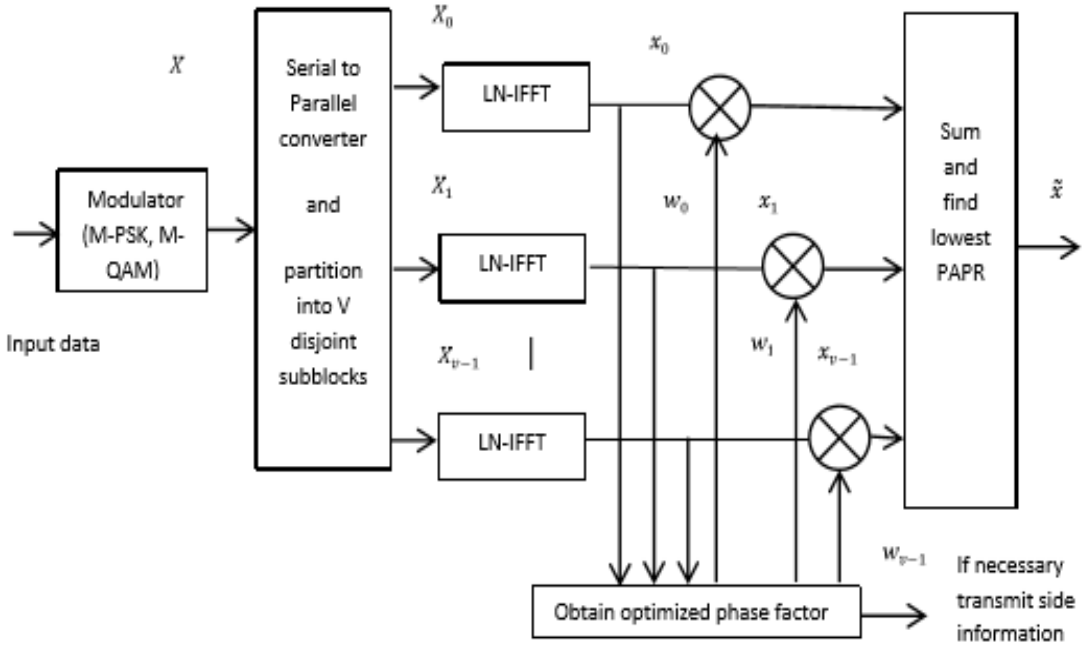


Figure2: A block diagram of PTS technique.

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CLIPPING AND FILTERING

High PAPR is a standout amongst the most widely recognized issues in OFDM. A high PAPR brings about limitations like increased complexity of the ADC and DAC and furthermore decreased efficiency of radio frequency (RF) power amplifier. One of the straightforward and, viable PAPR reduction strategies is clipping, which cancels out the signal component that exceed some constant amplitude called clip level.

In any case, clipping yields distortion power, which is called clipping noise, and expand the transmitted signal spectrum, which causes interference. Clipping is nonlinear process and causes in-band noise distortion, which causes degradation in the performance of bit error rate (BER) and out-of-band noise, which decrease the spectral efficiency [12].

Clipping and filtering technique is powerful in eliminating components of the expanded spectrum. Although filtering can diminish the spectrum development, filtering subsequent to clipping can decrease the out-of-band radiation, yet may likewise bring about some peak re-growth, which the peak signal exceed in the clip level. The strategy of iterative clipping and filtering diminishes the PAPR without spectrum expansion.

However, the iterative signal takes long time and it will increase the computational complexity of an OFDM transmitter. A block diagram of PAPR reduction scheme using clipping and filtering is shown in figure 3 [12]. Here N is the number of subcarrier.

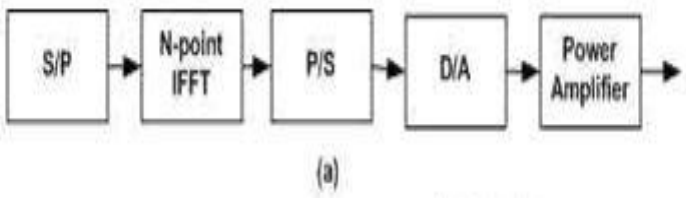


Figure 3: (a) OFDM system

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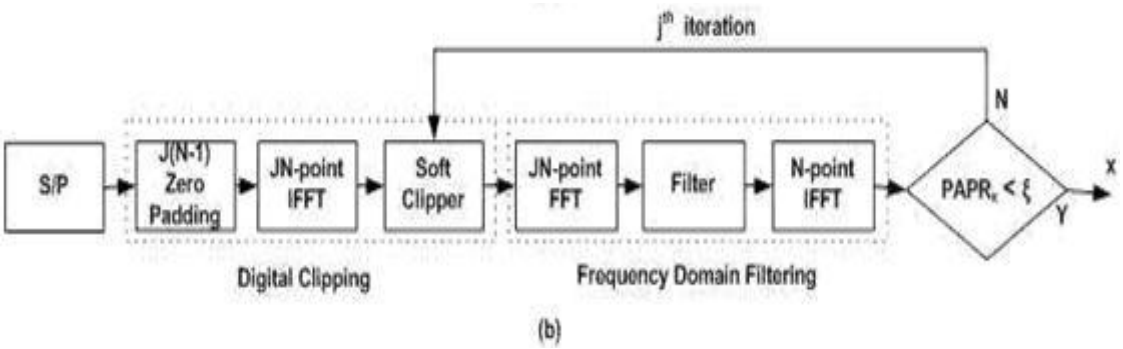


Figure 3: (b) Clipping and Filtering Block diagram.

DFT SPREADING

DFT –Spreading stands for Discrete Fourier Transform spreading, it involves the spreading of input signal with the help of DFT (Discrete Fourier Transform) operation which can be taken into IDFT. DFT Spreading results in reduction of PAPR of OFDM signal to the extent of single carrier transmission. Mobile terminal in uplink transmission make use of this technique. It is called as single carrier FDMA. The single carrier FDMA (SC-FDMA) is used for uplink transmission in 3GPP LTE standard [12]. DFT of identical size as IDFT is used as (spreading code). Then OFDMA system becomes equivalent to SC-FDMA system. The reasons being DFT and IDFT operations cancel each other. In this case the PAPR of transmitted signal will be same as single carrier system. In OFDMA framework, subcarrier are partitioned and allocated to multiple mobile user. In this case each terminal in uplink uses a subset of subcarrier to transmit its own data whereas it does not happen in case of downlink. The remaining subcarriers which are not used for their own transmission will be filled with zeros. The effect of PAPR reduction depends on the way of assuming the subcarrier to each terminal [6]. Here the input data x[m] is DFT spread to produce X[i] and then allocated as

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$$\tilde{x}[k] = \begin{cases} X[k/s] & k = s.m1, m1 = 0,1,2.....M-1 \\ 0 & otherwise \end{cases} \quad (12)$$

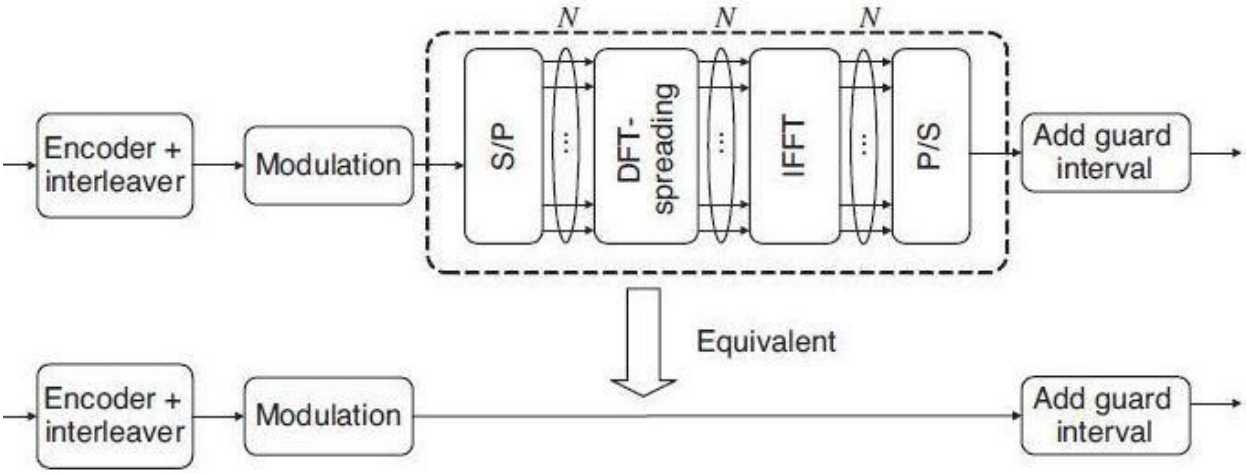


Figure 4: Equivalent of OFDMA system with DFT spreading code to a single-carrier system [12]

Selective Mapping

In this scheme, firstly M statistically independent input data symbols which represent the similar information are generated and then each sequence are processed by M parallel N-point complex IFFT to generate M different time-domain OFDM symbols. The symbol with the minimum PAPR is chosen for transmission. The key point of SLM method lies in how to generate multiple divergent time-domain OFDM symbols when the input data for transmission is the same. For this purpose, M pseudo-random phase rotation sequences $\Psi_m = [\Psi_{m,0} \quad \Psi_{m,1} \quad \dots \quad \Psi_{m,N-1}]^T$ with $m = 1, 2, \dots, M$ are defined; where $\Psi_{m,k} = e^{j\psi_{m,k}}$ and $\psi_{m,n}$ is uniformly distributed in $[0, 2\pi]$. This method can be seen as performing a dot product operation on the input tones $X(k)$ with rotation factor$e^{j\psi_{m,k}}$. In practice, all the elements of the phase sequence Ψ_1 are set to 1 to as to make this branch sequence the original OFDM symbol. A block diagram of SLM

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scheme is shown in figure 5 [13]. The selected phase sequence should be transmitted to receiver as side information to allow the recovery of original symbol sequence at the receiver which decreases the data transmission rate. The phase sequence p_m, 0<=m<=M-1 should be stored at both the transmitter and receiver .An erroneous detection of side information will cause the whole system to be damaged. Therefore a strong protection of side information is very essential.

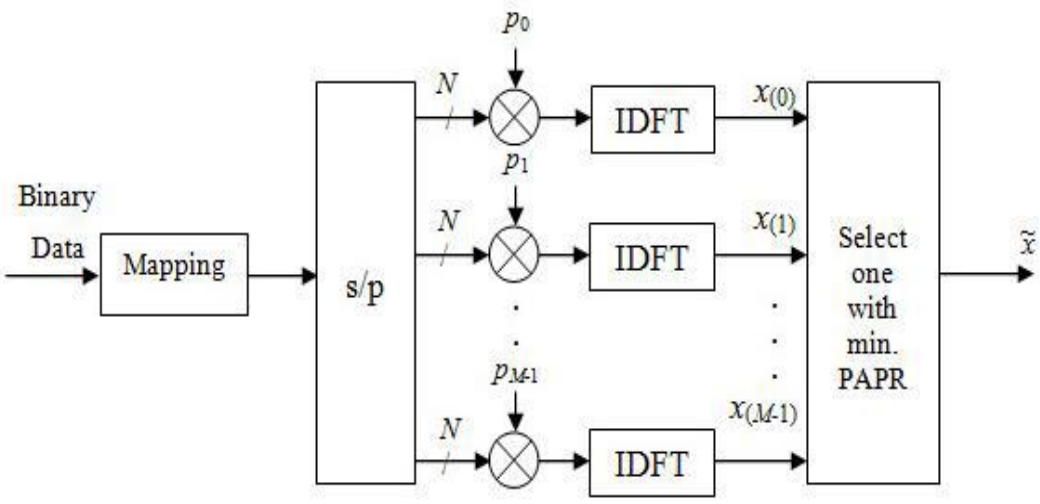


Figure 5: Block diagram SLM technique.

Comparison

A brief comparison of various PAPR reduction techniques has been depicted in the table 1.

Table 1

Reduction Scheme	Implementation Complexity	Data Rate Loss	Power Increase	BER Degradation
Clipping& Filtering				

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	MEDIUM-HIGH	NO	NO	YES
Selective Mapping (SLM)	VERY-HIGH	YES	NO	NO
Partial Transmit Sequence (PTS)	VERY-HIGH	YES	NO	YES
Tone Reservation (TR)	VERY-HIGH	YES	YES	NO
Tone Insertion (TI)	VERY-HIGH	YES	YES	YES

It is clear from the table 1, that none of the prior-art techniques have all the desired feature: very large CCDF(PAPR) reduction, very low implementation complexity, no loss of capacity, no increase of transmit power, and so forth.

CONCLUSION

OFDM is a remarkably attractive strategy for multicarrier transmission and has turned out to be one of the standard decisions for rapid speed transmission over a communication channel. It has various advantages; but has one noteworthy drawback, it has a high PAPR.

In this paper, a few numbers of the techniques for decreasing the high PAPR of the OFDM system were analyzed and compared. Among the techniques that were analyzed, it was found that, no particular PAPR reduction strategy is the best solution

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for the OFDM framework. Different parameters like loss in rate, transmit signal power increment, BER increase, computational complexity increment should to be taken into consideration before choosing the appropriate PAPR technique.

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